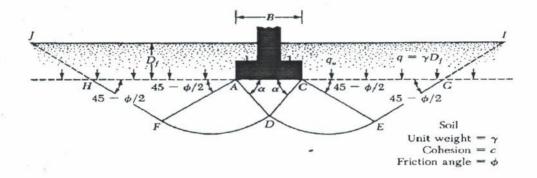
### MATERY OF SOIL MECHANIS -2

(Diktat Mekanika Tanah-2)

### MODUL - 1:

# Shear Strength Bearing Capacity

### Consolidation and Settlement



Idrus Ir. M.Sc

Staff Pengajar Jurusan Teknik Sipil FTSP – ISTN

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### I. KUAT GESER TANAH / SHEAR STRENGTH OF SOIL

The *shear strength* of a soil mass is the internal resistance per unit area that the soil mass can offer to resist failure and sliding along any plane inside it. Engineers must understand the nature of shearing resistance in order to analyze soil stability problems such as bearing capacity, slope stability, and lateral pressure on earth-retaining structures.

### Mohr-Coulomb Failure Criteria

Mohr (1900) presented a theory for rupture in materials. This theory contended that a material fails because of a critical combination of normal stress and shear stress, and not from either maximum normal or shear stress alone. Thus, the functional relationship between normal stress and shear stress on a failure plane can be expressed in the form

$$\tau_f = f(\sigma) \tag{8.1}$$

where

 $\tau_f$  = shear stress on the failure plane

 $\sigma$  = normal stress on the failure plane

The failure envelope defined by Eq. (8.1) is a curved line. For most soil mechanics problems, it is sufficient to approximate the shear stress on the failure plane as a linear function of the normal stress (Coulomb, 1776). This relation can be written as

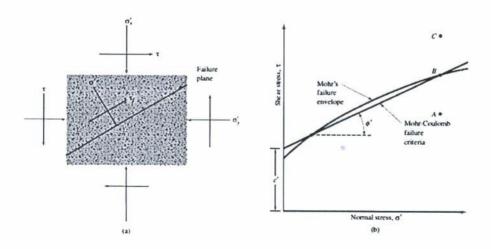
$$\tau_f = c + \sigma \tan \phi \tag{8.2}$$

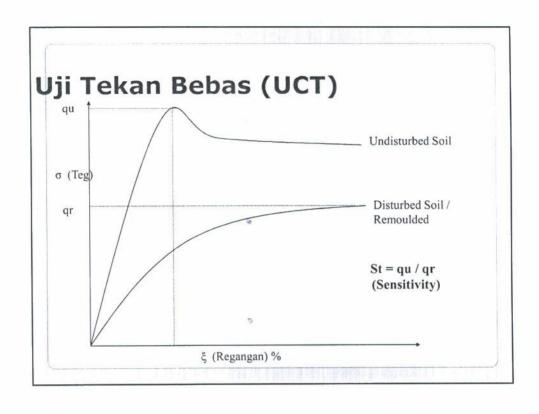
where

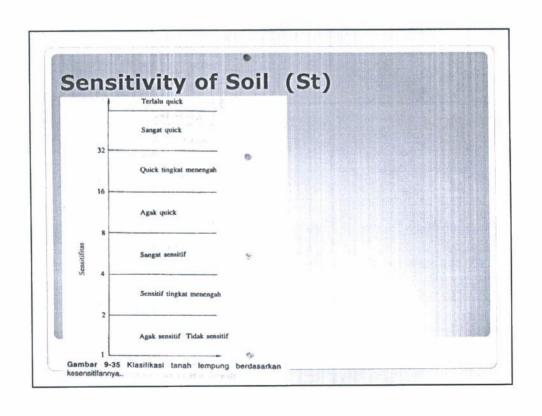
c = cohesion

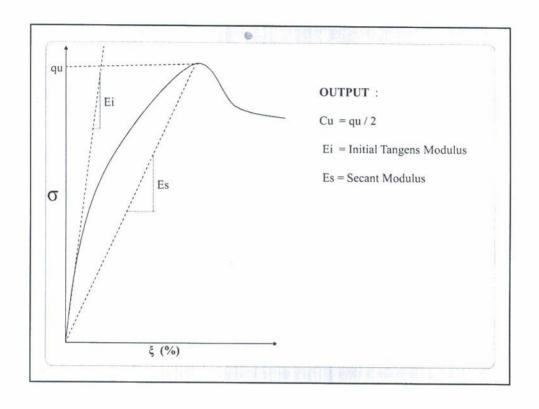
 $\phi$  = angle of internal friction

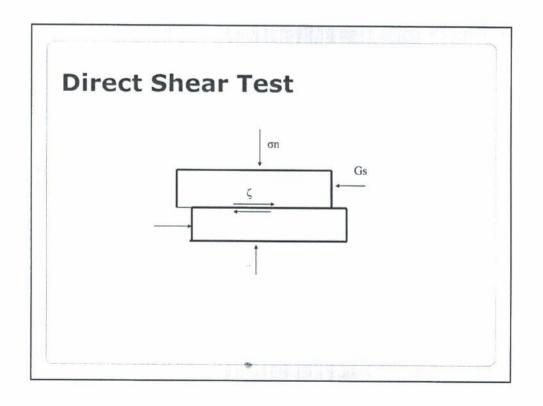
The preceding equation is called the Mohr-Coulomb failure criteria.

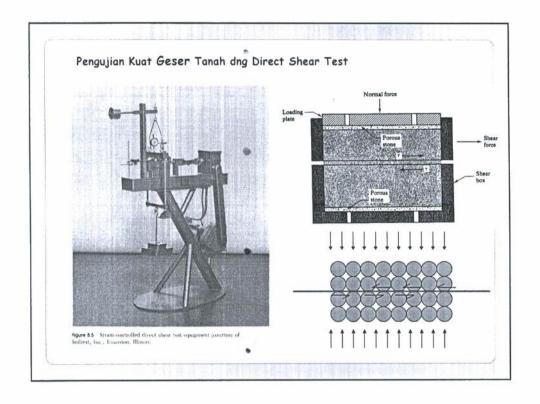


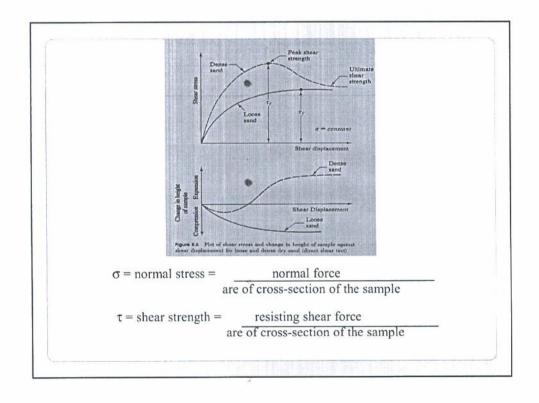




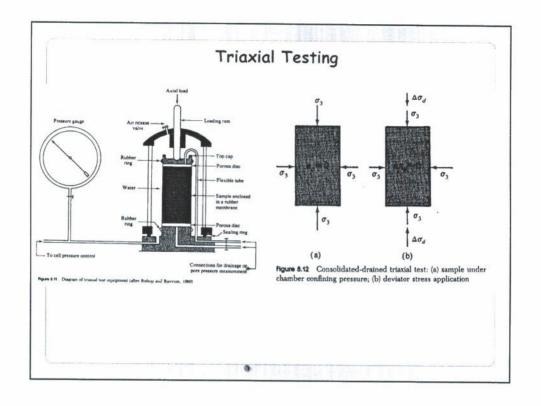








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# Type Triaxial Test di Laboratorium UU Test Uncosolidated Undrained CU Test Consolidated Undrained CD Test Consolidated Drained

# Tegangan-tegangan untuk pembuatan grafik Mohr Coulomb. Triaxial CU Test

CU TEST
$$\sigma 11' = (\Delta \sigma 11 + \sigma 31) - u1$$
 $\sigma 31' = \sigma 31 - u1$ 
 $u = Diukur$ 
 $\sigma 12' = (\Delta \sigma 12 + \sigma 32) - u2$ 
 $\sigma 32' = \sigma 32 - u2$ 

$$\sigma 13' = (\Delta \sigma 13 + \sigma 33) - u3$$
 $\sigma 33' = \sigma 33 - u3$ 

## Tegangan-tegangan untuk pembuatan grafik Mohr Coulomb. Triaxial CD Test

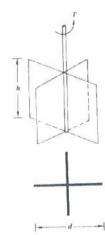
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• CD TEST \sigma 11' = (\Delta \sigma 11 + \sigma 31) - u1 \sigma 31' = \sigma 31 - u1 u1 = u2 = u3 = 0 \sigma 12' = (\Delta \sigma 12 + \sigma 32) - u2 (Karena drained) \sigma 32' = \sigma 32 - u2 \sigma 13' = (\Delta \sigma 13 + \sigma 33) - u3 \sigma 33' = \sigma 33 - u3
```

### UJI KUAT GESER DI LAPANGAN

UJI GESER VANE (BALING-BALING)

Uji ini khusus dilakukan pada kondisi lapisan tanah lempung lunak, dimana pertimbangannya adalah bahwa bila dilakukan pengambilan sample dengan tabung, maka akan terjadi disturbance / ketergangguan sample uji, sehingga tidak akurat lagi bila dikatakan undisturbed soil

### VANE SHAER TEST

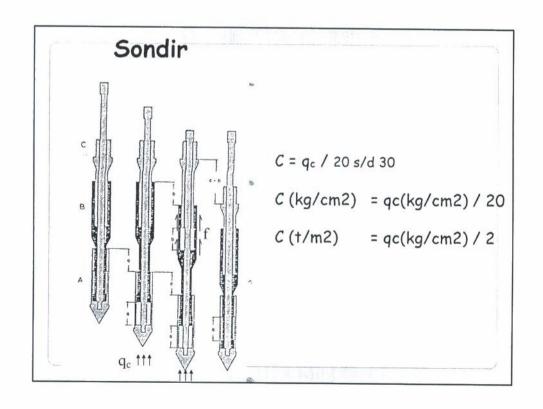


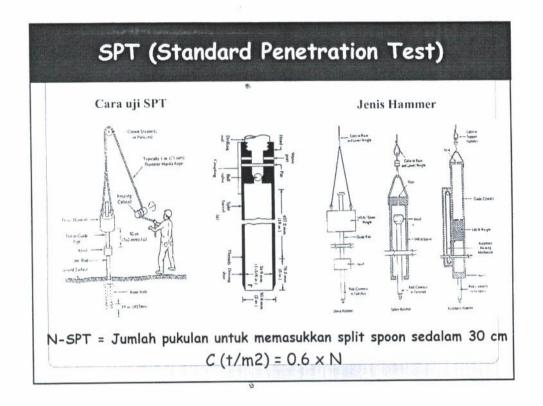
$$T = \pi c_u \left[ \frac{d^2 h}{2} + \beta \frac{d^3}{4} \right]$$

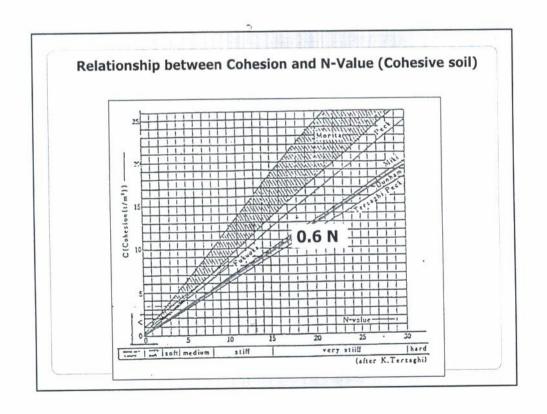
$$c_u = \frac{T}{\pi \left[ \frac{d^2h}{2} + \beta \frac{d^3}{4} \right]}$$

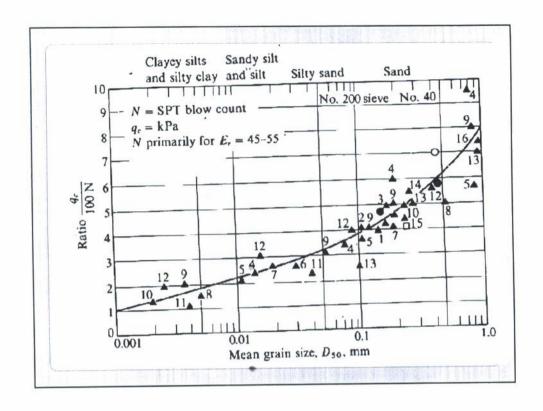
- β = 1/2 bila tahanan geser termobilisasi dianggap berbentuk segitiga
- β = 2/3 bila tahanan geser termobilisasi dianggap berbentuk seragam
- $\beta$  = 3/5 bila tahanan geser termobilisasi dianggap berbentuk parabola

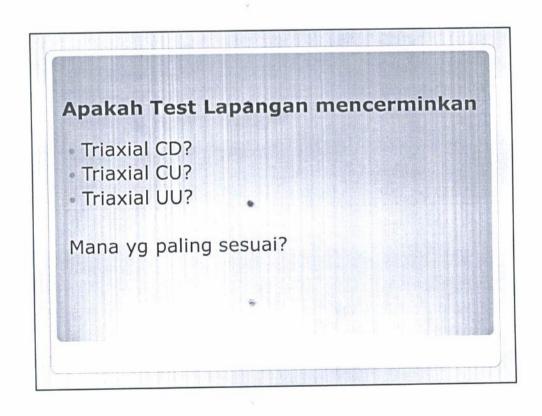
KORELASI SHEAR STRENGHT PARAMETER DENGAN DATA UJI LAPANGAN (qc dan N SPT)

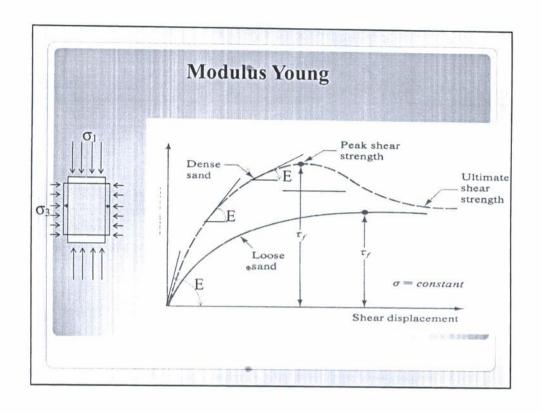


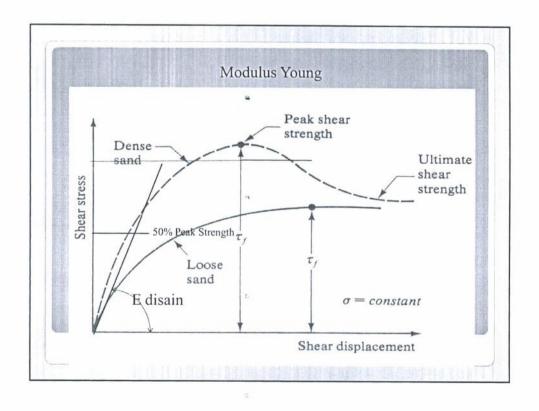


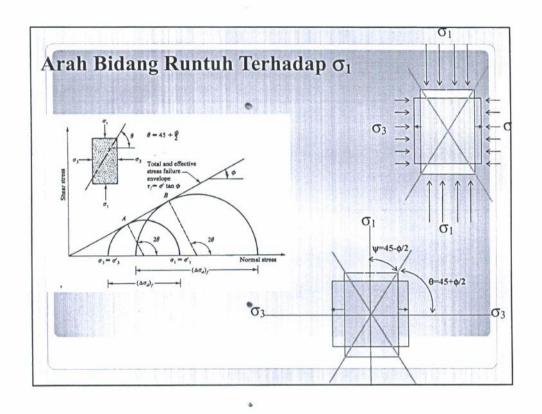


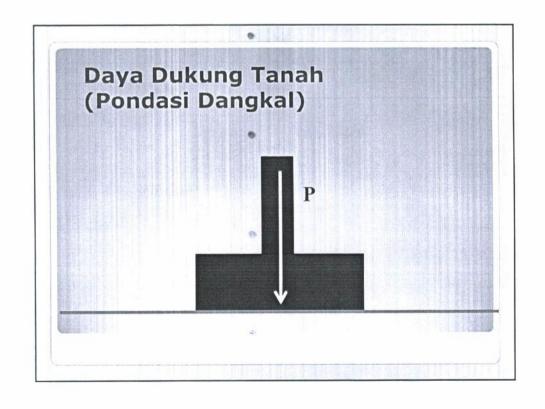


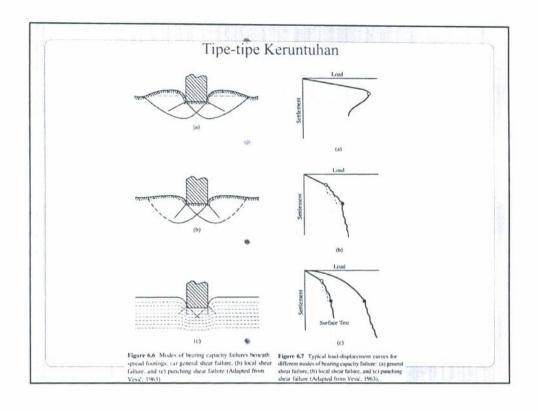


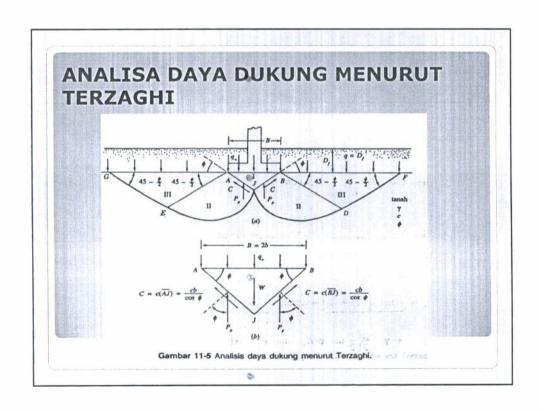


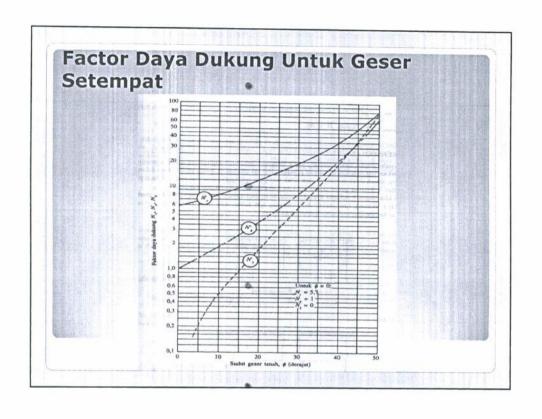


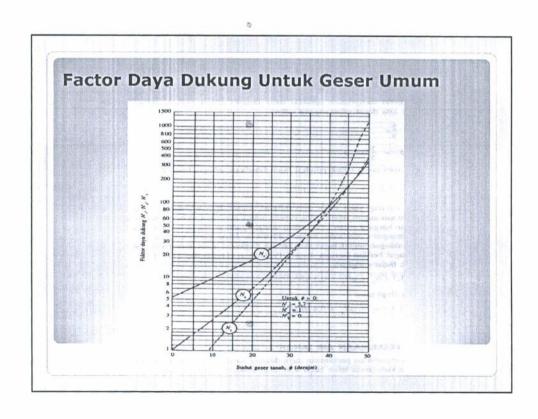












### Terzaghi

Using the equilibrium analysis, Terzaghi expressed the ultimate bearing capacity

$$q_* = cN_c + qN_s + \frac{1}{2}\gamma BN_\gamma$$
 (strip foundation) (3.3)

where

c = cohesion of soil  $\gamma$  = unit weight of soil

 $\gamma$  = unit weight of soft  $q = \gamma D_f$   $Q = \gamma D_f$ functions of the soil friction angle,  $\phi$ 

The bearing capacity factors,  $N_c$ ,  $N_q$ , and  $N_y$  are defined by

$$N = \cot \phi \left[ \frac{e^{2G\sigma/4 - \phi/2 \cos \phi}}{2 \cos^2 \left( \frac{\pi}{4} + \frac{\phi}{2} \right)} - 1 \right] = \cot \phi (N_4 - 1)$$
(3.4)

$$N_{\epsilon} = \frac{e^{2C\pi/4} \cdot e^{27\mu\omega\phi}}{2\cos^2\left(45 + \frac{\phi}{2}\right)}$$
 (3.5)

$$N_s = \frac{1}{2} \left( \frac{K_{p_s}}{\cos^2 \phi} - 1 \right) \tan \phi$$
(3.6)

where  $K_{py}$  = passive pressure coefficient

$$q_{\nu} = cN_c + qN_q + \frac{1}{2}\gamma BN_{\text{eff}}$$
 (strip foundation) (3.3)

where

c =cohesion of soil

 $\gamma$  = unit weight of soil

 $q = \gamma D_f$   $N_c$ ,  $N_q$ ,  $N_y$  = bearing capacity factors that are nondimensional and are only functions of the soil friction angle,  $\phi$ 

The bearing capacity factors,  $N_c$ ,  $N_q$ , and  $N_\gamma$  are defined by

$$N_{\epsilon} = \cot \phi \left[ \frac{e^{2(3\varepsilon/4 - \phi/2)\tan \phi}}{2\cos^2\left(\frac{\pi}{4} + \frac{\phi}{2}\right)} - 1 \right] = \cot \phi (N_{\epsilon} - 1)$$
(3.4)

$$q_v = 1.3cN_c + qN_e + 0.4\gamma BN_{\gamma}$$
 (square foundation) (3.7)

$$q_{\nu} = 1.3cN_c + qN_q + 0.3\gamma BN_{\gamma}$$
 (circular foundation) (3.8)

### Example

3.2

Repeat Example Problem 3.1, assuming local shear failure occurs in the soil supporting the foundation.

### Solution

From Eq. (3.10)

$$q_u = 0.867cN'_c + qN'_u + 0.4\gamma BN'_{\gamma}$$

From Figure 3.5, for  $\phi = 20^{\circ}$ 

$$N_c' = 12$$

$$N_a' = 4$$

$$N_{7}' = 1.7$$

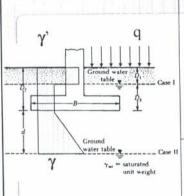
So

$$q_{\nu} = (0.867)(15.2)(12) + (1 \times 17.8)(4) + (0.4)(17.8)(1.5)(1.7)$$

$$= 158.1 + 71.2 + 18.2 = 247.5 \text{ kN/m}^2$$

$$q_{\rm all} = \frac{247.5}{4} = 61.9 \text{ kN/m}^2$$

Allowable gross load =  $Q = (q_{all})(B^2) = (61.9)(1.5^2) = 139 \text{ kN}$ 



### Case I

If the water table is located so that  $0 \le D_1 \le D_f$ , the factor q in the bearing capacity equations takes the form

$$q = \text{effective surcharge} = D_1 \gamma + D_2 (\gamma_{\text{od}} - \gamma_{\text{k}})$$

where  $\gamma_{set} = \text{saturated unit weight of soil}$  $\gamma_w = \text{unit weight of water}$ 

Also, the value of  $\gamma$  in the last term of the equations has to be replaced by  $\gamma'$  = y ... - y ..

For a water table located so that  $0 \le d \le B$ ,

(3.13)

The factor  $\boldsymbol{\gamma}$  in the last term of the bearing capacity equations must be replaced by the factor

 $\bar{\gamma} = \gamma' + \frac{d}{R}(\gamma - \gamma')$ 

(3.14)

(3.12)

When the water table is located so that  $d \ge B$ , the water will have no effect on the ultimate bearing capacity.

### **Bearing Capacity Factors**

Based on laboratory and field studies of bearing capacity, the basic nature of the failure surface in soil suggested by Terzaghi now appears to be correct (Vesic, 1973). However, the angle  $\alpha$  as shown in Figure 3.5 is closer to  $45 + \phi/2$  than to  $\phi$ . If this change is accepted, the values of  $N_c$ ,  $N_q$ , and  $N_r$  for a given soil friction angle will also change from those given in Table 3.1. With  $\alpha = 45 + \phi/2$ , the relations for  $N_c$  and  $N_q$  can be derived as

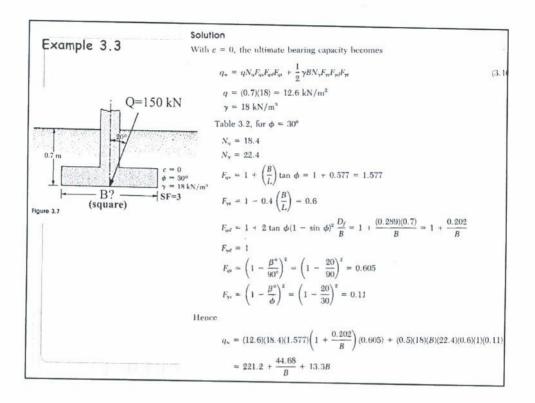
$$N_{q} = \tan^{2}\left(45 + \frac{\phi}{2}\right)e^{\pi \tan \phi} \tag{3.26}$$

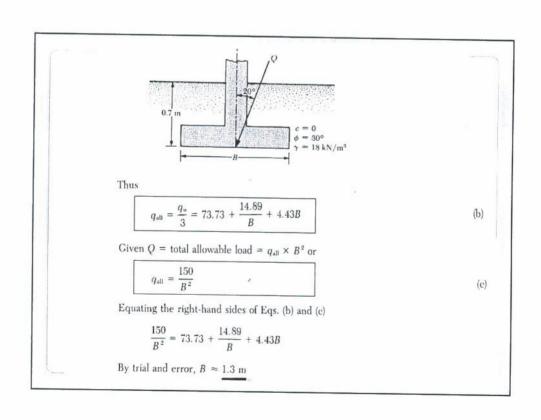
$$N_{\epsilon} = (N_{q} - 1)\cot\phi \tag{3.27}$$

The equation for  $N_e$  given by Eq. (3.27) was originally derived by Prandtl (1921), and the relation for  $N_e$  [Eq. (3.26)] was presented by Reissner (1924). Caquot and Kerisel (1953) and Vesic (1973) gave the relation for  $N_{\gamma}$  as

$$N_{\gamma} = 2(N_{q} + 1)\tan\phi \tag{3.28}$$

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Example

3.1

A square foundation is  $1.5 \text{ m} \times 1.5 \text{ m}$  in plan. The soil supporting the foundation has a friction angle of  $\phi = 20^{\circ}$  and  $c = 15.2 \text{ kN/m}^2$ . The unit weight of soil,  $\gamma$ , is  $17.8 \text{ kN/m}^3$ . Determine the allowable gross load on the foundation with a factor of safety (FS) of 4. Assume the depth of the foundation  $(D_f)$  to be one meter, and general shear failure occurs in soil.

1.0 m

1.5 x 1.5 m

### Solution

From Eq. (3.7)

$$q_n = 1.3cN_r + qN_q + 0.4\gamma BN_\gamma$$

From Figure 3.4, for  $\phi = 20^{\circ}$ 

 $N_c = 17.7$ 

 $N_{g} = 7.4$ 

V<sub>\*</sub> = 5

Thus

$$\begin{split} q_n &= (1.3)(15.2)(17.7) + (1\times17.8)(7.4) + (0.4)(17.8)(1.5)(5) \\ &= 349.75 + 131.72 + 53.4 = 534.87 \approx 535 \text{ kN/m}^2 \end{split}$$

So, allowable load per unit area of the foundation =

$$q_{\text{all}} = \frac{q_n}{FS} = \frac{535}{4} = 133.75 \text{ kN/m}^2$$

Thus, the total allowable gross load

$$Q = (133.75)B^2 = (133.75)(1.5 \times 1.5) = 300.9 \approx 300 \text{ kN}$$

The factor of safety as defined by Eq. (3.40) may be referred to as the net allowable bearing capacity. This should be kept at least about 3 in all cases.

Another type of factor of safety for the bearing capacity of shallow foundations is often used. This is the factor of safety with respect to shear failure  $(FS_{\text{shear}})$ . In most cases, a value of  $FS_{\text{shear}} = 1.4$ –1.6 is desirable along with a minimum factor of safety of 3–4 against gross or net ultimate bearing capacity. In order to calculate the net allowable load on the basis of a given  $FS_{\text{shear}}$ , the following procedure should be adopted:

1. Let c and  $\phi$  be the cohesion and the angle of friction of soil, and let  $FS_{\text{theor}}$  be the required factor of safety with respect to shear failure. So, the developed cohesion and the angle of friction can be given as

$$c_d = \frac{c_l}{ES_L} \tag{3.41}$$

$$\phi_d = \tan^{-1} \left( \frac{\tan \phi}{ES} \right)^{-\epsilon}$$
(3.42)

2. The gross allowable bearing capacity can now be calculated according to Eqs. (3.3), (3.7), (3.8) or the general bearing capacity equation [Eq. (3.16)] using  $c_d$  and  $\phi_d$  as the shear strength parameters of the soil. For example, the gross allowable bearing capacity of a continuous foundation according to Terzaghi's equation can be written as

$$q_{\text{all}} = c_{\theta}N_{e} + qN_{q} + \frac{1}{2}\gamma BN_{q}$$
 (3.43)

where  $N_c$ ,  $N_q$ , and  $N_{\gamma}$  = bearing capacity factors for friction angle,  $\phi_d$ 

3. The net allowable bearing capacity is thus

$$q_{\text{octable}} = q_{\text{alt}} - q = c_{\theta}N_c + q(N_{\theta} - 1) + \frac{1}{2}\gamma BN_{\phi}$$
 (3.44)

3.7 Eccentrically Loaded Foundations

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pressure distribution on the soil will be as shown in Figure 3.8a. The value of  $q_{\rm max}$  can be given by the expression

$$q_{\text{max}} = \frac{4Q}{3L(B - 2c)}$$
(3.49)

2. Determine the effective dimensions of the foundation as

$$B' = \text{effective width} = B - 2e$$
  
 $L' = \text{effective length} = L$ 

Note that, if the eccentricity is in the direction of the length of the foundation, the value of L' would be equal to L-2e. The value of B' would be equal to B. The smaller of the two dimensions (that is, L' and B') is the effective width of the foundation.

3. Use Eq. (3.16) for the ultimate bearing capacity as

$$q'_{\theta} = cN F_{ij}F_{cd}F_{ci} + qN_{q}F_{ij}F_{qi}F_{qi} + \frac{1}{2}\gamma B^{\alpha}N_{\beta}F_{ji}F_{ji}F_{ji}$$
 (3.50)

For the evaluation of  $F_c$ ,  $F_{ur}$ ,  $F_{yr}$ ,  $F_{dr}$ ,  $F_{gr}$ , and  $F_{yr}$ . Equations (3.20) to (3.22) and Eqs. (3.29) to (3.33) have to be used with *effective length* and *effective width* dimensions in place of L and B, respectively.

For determination of  $F_{cd}$ ,  $F_{\eta d}$ , and  $F_{\eta d}$ , use Equations (3.23) to (3.28) (do\_not replace B with B').

4. The total ultimate load that the foundation can sustain is

$$Q_{dt} = q_{*}(B')(L')$$
 (3.51)

5. The factor of safety against bearing capacity failure is given as

$$FS = \frac{Q_{ab}}{Q}$$
 (3.52)

As we can see, eccentricity tends to decrease the load-bearing capacity of a foundation. In such cases, it is probably advantageous to place the foundation columns off center, as shown in Figure 3.9. This, in effect, produces a centrally loaded foundation with uniformly distributed pressure.

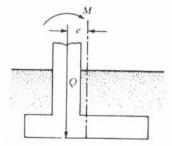
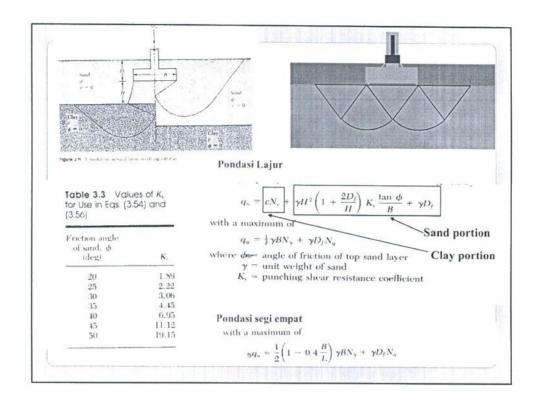
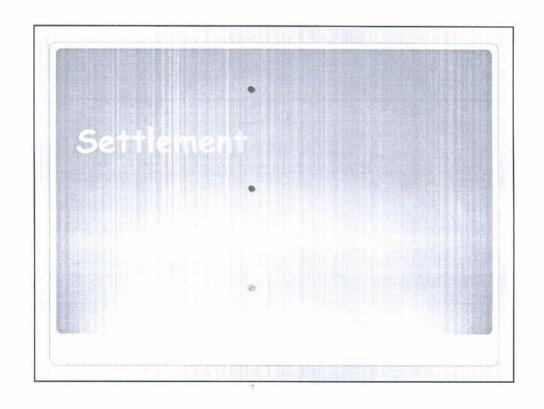
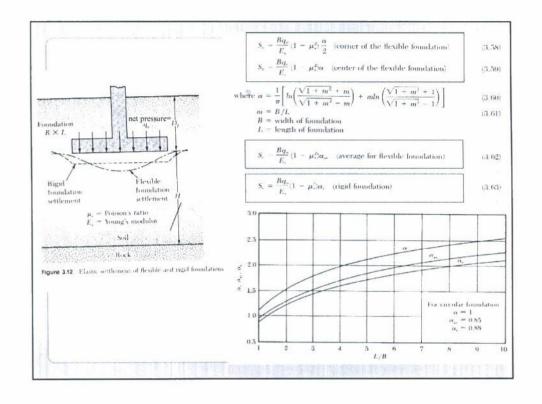
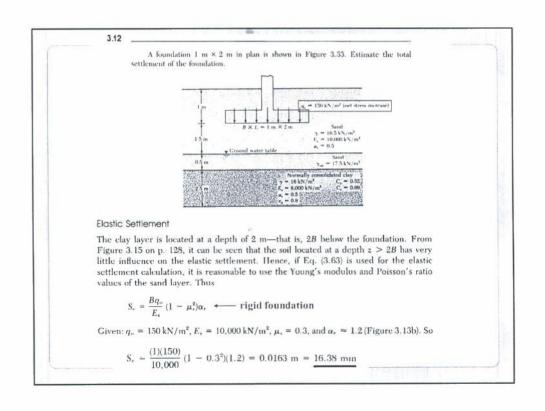


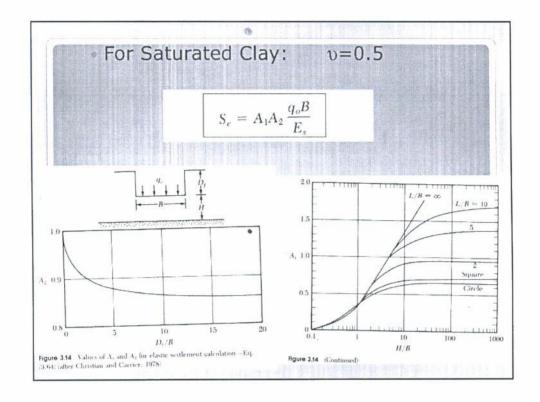
Figure 3.9 Foundation of columns with off-center loading

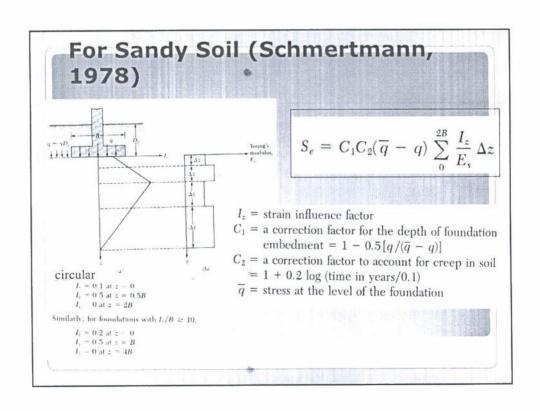


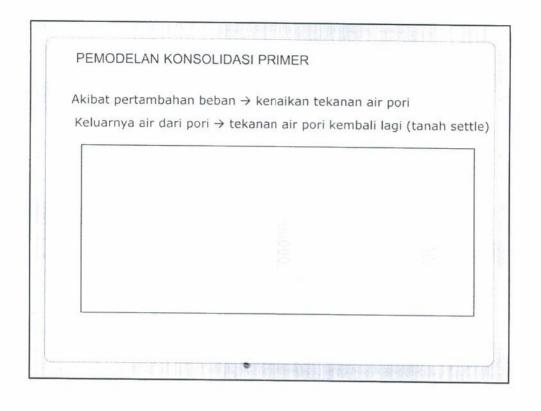


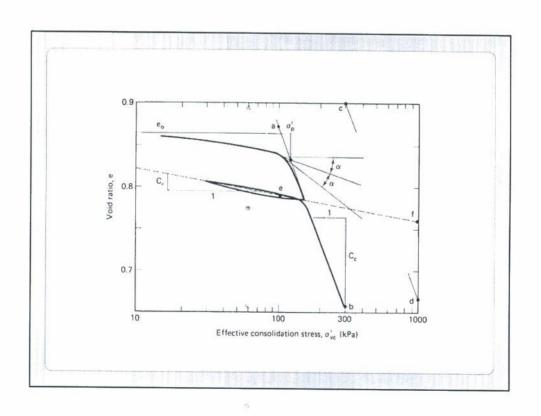












### **CONSOLIDATION SETTLEMENT**

- Total Settlement (St) = Si + Scp + Scs
- Si = Immediately Settlement
- Scp = Primary Consolidation Settlement
- Scs = Secondary Consolidation
   Settlement

Untuk lempung yang terkonsolidasi normal (Normally Consolidation) dimana

Pc < Po, maka

 $Sep = (Ce.H/1+eo) log (Po+\Delta P/Po)$ 

Bila Pc> Po (Lempung yang Over Konsolidasi ) maka terdapat 2 (dua) kemungkinan

Bila Po+ $\Delta$ P < Pc dan Po+ $\Delta$ P > Pc

 $Po + \Delta P < Pc$ 

Scp =(Cs.H/1+eo) log (Po+ $\Delta$  P/Po)

 $Po + \Delta P > Pc$ 

 $Sep = (Cs.H/1+eo) log (Pe/Po) + (Cc.H/1+eo) log (Po+\Delta P/Pc)$ 

